

NA2012 WEEK 13 LAB EXERCISES

PROBLEM 1

$$A = \begin{bmatrix} 1 & 2 \\ 2 & 5 \end{bmatrix}$$

- Calculate the biggest eigenvalue of the matrix by hand by using power method
- Calculate the smallest eigenvalue of the matrix by hand by using inverse power method
- Check your result by using computer programs NA131, NA133

PROBLEM 2

$$A = \begin{bmatrix} \sigma_x & \tau_{xy} & \tau_{xz} \\ \tau_{yx} & \sigma_y & \tau_{yz} \\ \tau_{zx} & \tau_{zy} & \sigma_z \end{bmatrix} = \begin{bmatrix} 10 & 4 & -6 \\ 4 & -6 & 8 \\ -6 & 8 & 14 \end{bmatrix} \text{ MPa}$$

Normal and shear stresses are given. Find the principle stresses

- Biggest eigenvalue by power method
- By Jacobi method

PROBLEM 3

Find the roots of $f(x) = x^3 - 3x^2 + 3x - 1$. First create the companion matrix and then solve the eigenvalues by computer

NA2011 WEEK 12 HOMEWORKS

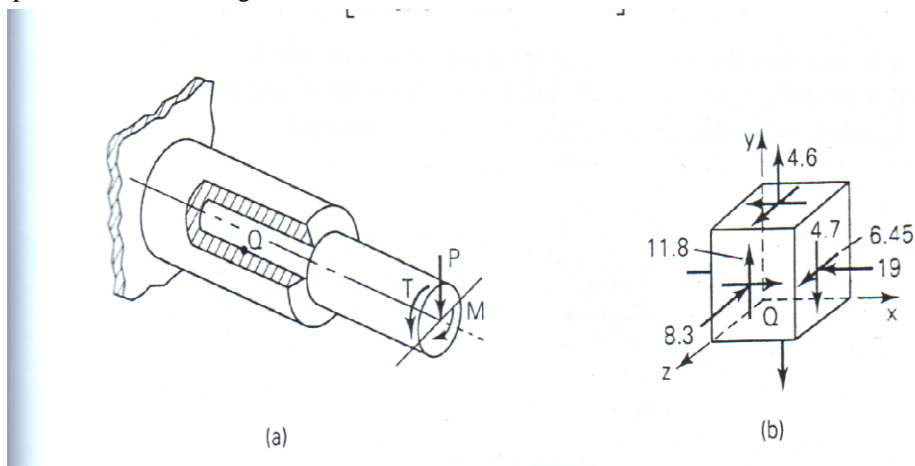
PROBLEM 1

A steel shaft is placed inside of a iron base as shown in the figure . T torsion and M bending moment is applied to the shaft. Under this forces stress matrix at point Q is as follows (Mpa)

$$\begin{bmatrix} -19 & -4.7 & 6.45 \\ -4.7 & 4.6 & 11.8 \\ 6.45 & 11.8 & -8.3 \end{bmatrix}$$

Calculate the principle stresses at point Q

Note : Principle stresses are the eigenvalues of the matrix



- Solve dominant principle stress (eigenvalue) by hand by using power method
- Solve smallest principle stress (eigenvalue) by hand by using inverse power method
- Solve all eigenvalues by computer by using Jacobi method

PROBLEM 2

Find the roots of $f(x) = x^4 - 4x^3 + 6x^2 - 4x + 1$. First create the companion matrix and then solve the eigenvalues by computer

PROBLEM 3

Calculate largest and smallest eigenvalues of the given matrix by using power method and inverse power method by hand

$$A = \begin{bmatrix} 2 & 8 & 10 \\ 8 & 4 & 5 \\ 10 & 5 & 17 \end{bmatrix}$$